

# Evaluating Absolute Value Functions

The absolute value of a real number  $x$  is defined by the following:

$$|x| = \begin{cases} x & \text{if } x \geq 0 \\ -x & \text{if } x \leq 0 \end{cases}$$

Note that the effect of taking the absolute value of a number is to strip away the minus sign if the number is negative and to leave the number unchanged if it is nonnegative.

Thus,  $|x| \geq 0$  for all values of  $x$ .

## Example

Evaluate various absolute value functions.

**1.** Evaluate  $|-2(5-1)|$

**2.** Is  $|-2+7| = |-2| + |7|$ ?

Evaluate each side of the equation to check your answer.

Is  $|x + y| = |x| + |y|$  for all real numbers  $x$  and  $y$ ?

If not, when will  $|x + y| = |x| + |y|$ ?

**3.** Is  $|\frac{6-9}{1+3}| = |\frac{6-9}{1+3}|$ ?

Evaluate each side of the equation to check your answer. Investigate with more examples, and decide if you think  $|x / y| = |x| / |y|$

**Before Starting** There may be differences in the results of calculations and graph plotting depending on the setting. Return all settings to the default value and delete all data.

### Step & Key Operation

(When using EL-9650/9600c)

\*Use either pen touch or cursor to operate.

### Display

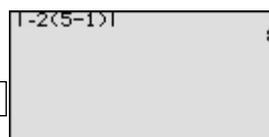
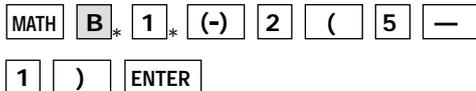
(When using EL-9650/9600c)

### Notes

**1-1** Access the home or computation screen.

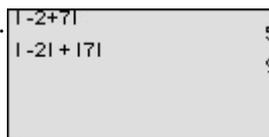
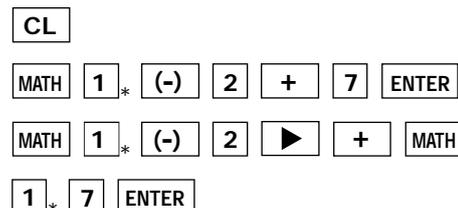


**1-2** Enter  $y = -2(5-1)$  and evaluate.



The solution is  $\pm 8$ .

**2-1** Evaluate  $|-2 + 7|$ . Evaluate  $|-2| + |7|$ .



$|-2 + 7| = 5$ ,  $|-2| + |7| = 9$   
 $\rightarrow |-2 + 7| \neq |-2| + |7|$ .

**Step & Key Operation**

(When using EL-9650/9600c)  
\*Use either pen touch or cursor to operate.

**Display**

(When using EL-9650/9600c)

**Notes**

**2.2** Is  $|x + y| = |x| + |y|$ ? Think about this problem according to the cases when  $x$  or  $y$  are positive or negative.

If  $x \geq 0$  and  $y \geq 0$   
[e.g.;  $(x, y) = (2, 7)$ ]

$$\begin{aligned} |x+y| &= |2 + 7| = 9 \\ |x|+|y| &= |2| + |7| = 9 \end{aligned}$$

$$\rightarrow |x + y| = |x| + |y|.$$

If  $x \leq 0$  and  $y \geq 0$   
[e.g.;  $(x, y) = (-2, 7)$ ]

$$\begin{aligned} |x+y| &= |-2 + 7| = 5 \\ |x|+|y| &= |-2| + |7| = 9 \end{aligned}$$

$$\rightarrow |x + y| \neq |x| + |y|.$$

If  $x \geq 0$  and  $y \leq 0$   
[e.g.;  $(x, y) = (2, -7)$ ]

$$\begin{aligned} |x+y| &= |2-7| = 5 \\ |x|+|y| &= |2| + |-7| = 9 \end{aligned}$$

$$\rightarrow |x + y| \neq |x| + |y|.$$

If  $x \leq 0$  and  $y \leq 0$   
[e.g.;  $(x, y) = (-2, -7)$ ]

$$\begin{aligned} |x+y| &= |-2-7| = 9 \\ |x|+|y| &= |-2| + |-7| = 9 \end{aligned}$$

$$\rightarrow |x + y| = |x| + |y|.$$

Therefore  $|x+y|=|x|+|y|$  when  $x \geq 0$  and  $y \geq 0$ , and when  $x \leq 0$  and  $y \leq 0$ .

**3.1** Evaluate  $\left| \frac{6-9}{1+3} \right|$ . Evaluate  $\frac{|6-9|}{|1+3|}$ .

CL MATH 1 \* a/b 6 - 9

▶ \* 1 + 3 ENTER

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MATH 1 \* 1 + 3 ENTER



$$\left| \frac{6-9}{1+3} \right| = 0.75, \quad \frac{|6-9|}{|1+3|} = 0.75$$

$$\rightarrow \left| \frac{6-9}{1+3} \right| = \frac{|6-9|}{|1+3|}$$

**3.2** Is  $|x / y| = |x| / |y|$ ? Think about this problem according to the cases when  $x$  or  $y$  are positive or negative.

If  $x \geq 0$  and  $y \geq 0$   
[e.g.;  $(x, y) = (2, 7)$ ]

$$\begin{aligned} |x/y| &= |2/7| = 2/7 \\ |x|/|y| &= |2| / |7| = 2/7 \end{aligned}$$

$$\rightarrow |x / y| = |x| / |y|$$

If  $x \leq 0$  and  $y \geq 0$   
[e.g.;  $(x, y) = (-2, 7)$ ]

$$\begin{aligned} |x/y| &= |(-2)/7| = 2/7 \\ |x|/|y| &= |-2| / |7| = 2/7 \end{aligned}$$

$$\rightarrow |x / y| = |x| / |y|$$

If  $x \geq 0$  and  $y \leq 0$   
[e.g.;  $(x, y) = (2, -7)$ ]

$$\begin{aligned} |x/y| &= |2/(-7)| = 2/7 \\ |x|/|y| &= |2| / |-7| = 2/7 \end{aligned}$$

$$\rightarrow |x / y| = |x| / |y|$$

If  $x \leq 0$  and  $y \leq 0$   
[e.g.;  $(x, y) = (-2, -7)$ ]

$$\begin{aligned} |x/y| &= |(-2)/-7| = 2/7 \\ |x|/|y| &= |-2| / |-7| = 2/7 \end{aligned}$$

$$\rightarrow |x / y| = |x| / |y|$$

The statement is true for all  $y \neq 0$ .

The EL-9650/9600c/9450/9400 shows absolute values with  $| \quad |$ , just as written on paper, by using the Equation editor. The nature of arithmetic of the absolute value can be learned through arithmetical operations of absolute value functions.